

# Multi-Attribute Auctions: Application to Workflow Management Systems

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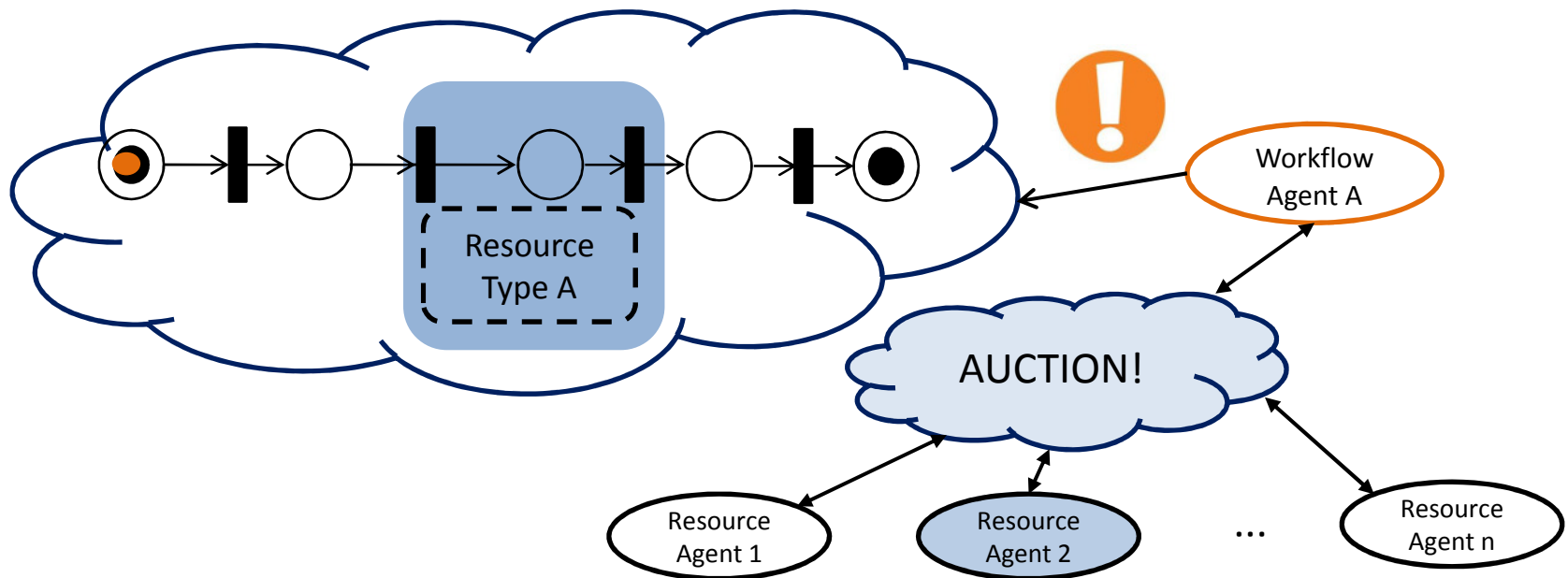


# Introduction



# Auctions in workflow management systems

- Auctions allow an optimal allocation for just-in-time:
  - Competitive market
  - Optimization according to a given criteria.



# Auctions in workflow management systems

- Just-in-time resource allocation
- Special domains:
  - Production not known in advance
  - Production under demand / Supply chain under demand
  - Handling unexpected tasks (provoked by faults)
  - Unknown resource status
  - Outsourced resources



# WMS: Multi-dimensional allocation problem

- Workflow managers are not only concerned by costs:
- Workflow managers are concerned about multiple attributes:
  - Economic costs
  - Product quality
  - Delivery times
  - Licenses / ISO standardizations
  - CO<sub>2</sub> emissions
  - Energy consumption
  - ...



# WMS: Multi-dimensional allocation problem

- Multi-criteria allocation problem
  - Number of attributes considered in the allocation  $> 1$
  - Modifying one attribute can condition the value of the rest
- Multi-attribute auctions
  - Number of attributes involved in the auction  $> 1$
  - Bids composed by several attributes.
  - Usually economic cost plus another attribute.
- Develop a multi-attribute auction mechanism for allocating resources and tasks in workflows



# Resource allocation in the supply chain issues

- Example: Smartphone manufacturer.
  - Needs to provide a bundle of smartphones in two days.  
Deadline = 2800 minutes
  - Sequentially outsources the manufacturing of the phone parts and ensembles them.
  - Maximum Budget = 200€

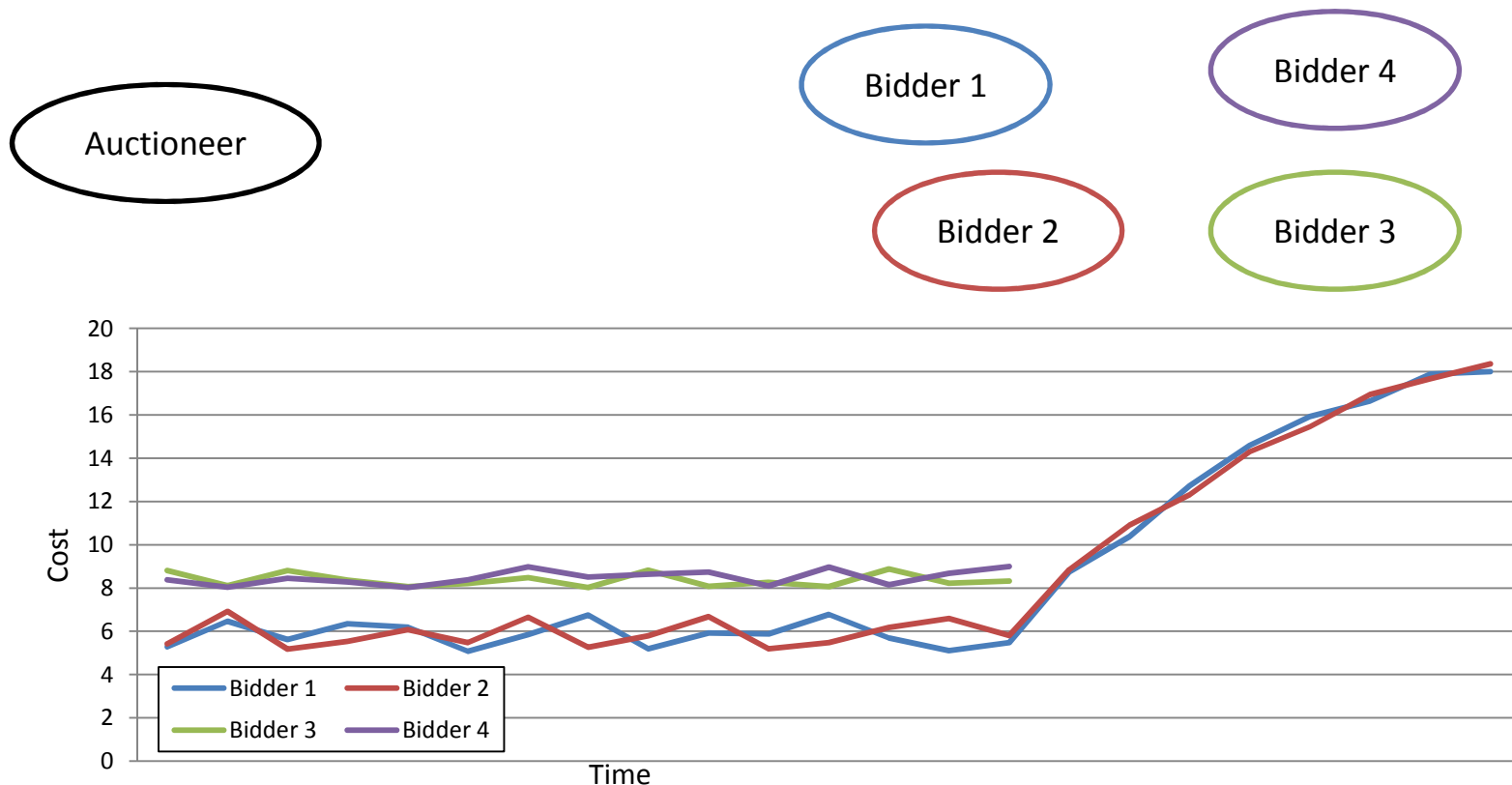


			Can invest	Can invest
Agreement:	900 mins 80 €	1000 mins 60 €	900 mins 60 €	800 mins
	850 mins 120 €	1200 mins 55 €		
Provided:	900 mins 80 €	1100 mins		



# Recurrent auctions issues

- Always the same participants in the market.
- **Bidder drop problem (BDP)**: Unsatisfied bidders leave the auction and the stronger bidders create an oligopoly.

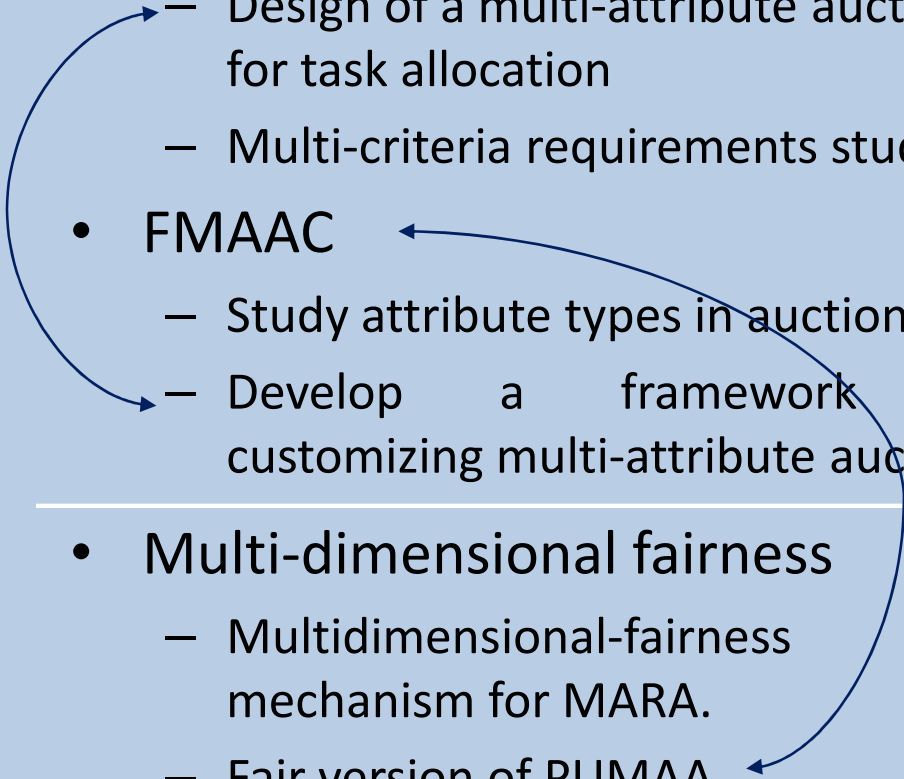


# Challenges

- Multi-attribute incentive compatibility
  - Encourage resource providers (RP) to reveal their **true values** in terms of **cost** and **attributes** (respect their agreements)
- Workflow related issues
  - **Misdelivered tasks**
  - Delays, budget problems, quality problems...
- Recurrent auctions' issues
  - **Bidder drop problem**
  - **Fairness** in multi-criteria problems



# Challenges vs. Contributions

- Multi-attribute IC
  - Workflow related issues
  - Recurrent auctions' issues
- PUMAA
    - Design of a multi-attribute auction for task allocation
    - Multi-criteria requirements study
  - FMAAC
    - Study attribute types in auctions
    - Develop a framework for customizing multi-attribute auctions
  - Multi-dimensional fairness
    - Multidimensional-fairness mechanism for MARA.
    - Fair version of PUMAA
    - Minimize the bidder drop problem
- 

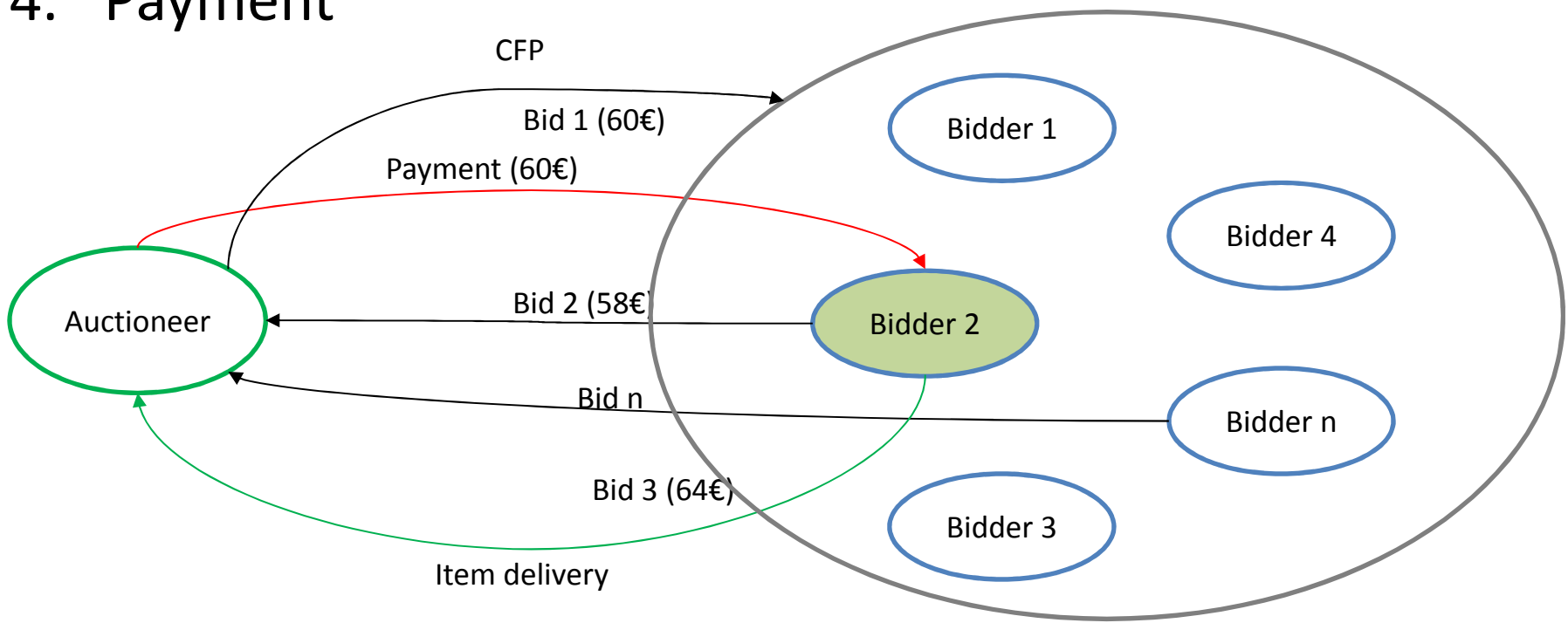


# Auctions for Multi-Attribute Resource Allocation (MARA)



# Background: Auction protocol steps

1. Call for proposals (CFP)
2. Bidding
3. Winner determination problem (WDP)
4. Payment



# Background: Auction Properties

- Mechanism Properties
  - Incentive Compatibility
    - Encourage truthful bidding
  - Efficiency
    - Best allocation possible
  - Buyer optimality
    - Best possible price
  - Individual-rationality
    - It is not harmful to participate
  - Budget-balance
    - No need of external subsidy
- Allocation properties
  - Social Welfare
    - Utilitarian
    - Egalitarian
  - Robustness
    - Reduce utility loss
    - Provide alternative solutions
  - Reliable
    - Confidence of success



# Auction state of the art

		Type			Auction Properties					Allocation Properties				Particularities			
		Sides	Items auctioned	1st / second price	Efficient	Incentive Compatible	Buyer-optimal	Individually rational	Budget Balance	BDP considered (fairness)	Robustness	Reliability	Social Welfare	Multi-criteria WDP	Bidder's attributes	Task allocation suitable	Procurement suitable
UniAttribute	Vickrey Auction	One	1	2	✓	✓	X	✓	✓	X	X	X	Util.	X	1	✓	✓
	MU Discriminatory Vickrey	One	n of the same type	2	✓	X	X	✓	✓	X	X	X	Util.	X	1	✓	✓
	MU non Discriminatory Vickrey	One	n of the same type	2	✓	✓	X	✓	✓	X	X	X	Util.	X	1	✓	✓
	VCG Auction	One	n	2	✓	✓	X	✓	✓	X	X	X	Util.	X	1	✓	✓
	GSP	One	n	2	X	X	X	✓	✓	X	X	X	Util.	X	1	?	?
	Google GSP	One	n	2	✓	✓	X	✓	✓	X	X	X	Util.	X	1	?	?
Multi-attribute	Che's first-score	One	1	1	X	X	✓	✓	✓	X	X	X	Util.	✓	n	✓	✓
	Che's second-score	One	1	2	✓	✓	X	✓	✓	X	X	X	Util.	✓	n	✓	✓
	Che's second-preferred-offer	One	1	2	✓	X	X	✓	✓	X	X	X	Util.	✓	n	✓	✓
	Parkes Modified VCG	One	1	English 1st	✓	Nash-Bayes	X	✓	✓	X	X	X	Util.	✓	n	X	✓
	David's English auction	One	1	English 2nd	✓	✓	X	✓	✓	X	X	X	Util.	✓	n	X	✓
	PERA	One	1	depends	✓	depends	depends	✓	✓	X	X	X	Util.	✓	n	X	✓
	De Smet auction	One	1	depends	✓	depends	depends	✓	✓	X	X	X	Util.	✓	n	X	✓
	Mahr unknwn utility func.	One	1	2	✓	X	X	✓	✓	X	X	X	Util.	✓	n	✓	✓
	VCG trust extension	One	1	2	X	X	X	✓	✓	X	✓	X	Util.	✓	2	✓	✓
	Porter's fault tolerant	One	1	2	✓	✓	X	✓	✓	X	✓	✓	Util.	✓	2	✓	✓
	Ramchurn's trust	One	1	2	✓	✓	X	✓	✓	X	✓	~	Util.	✓	2	✓	✓
		One	n	2	✓	✓	X	✓	✓	X	X	X	Util.	X	2	✓	✓
	Zhao's double auction	Double	n	2	✓	✓	X	✓	✓	X	X	X	Util.	X	2	✓	✓
	PUMAA	One	1	2	✓	✓	X	✓	✓	X	✓	~	Util.	✓	n	✓	✓



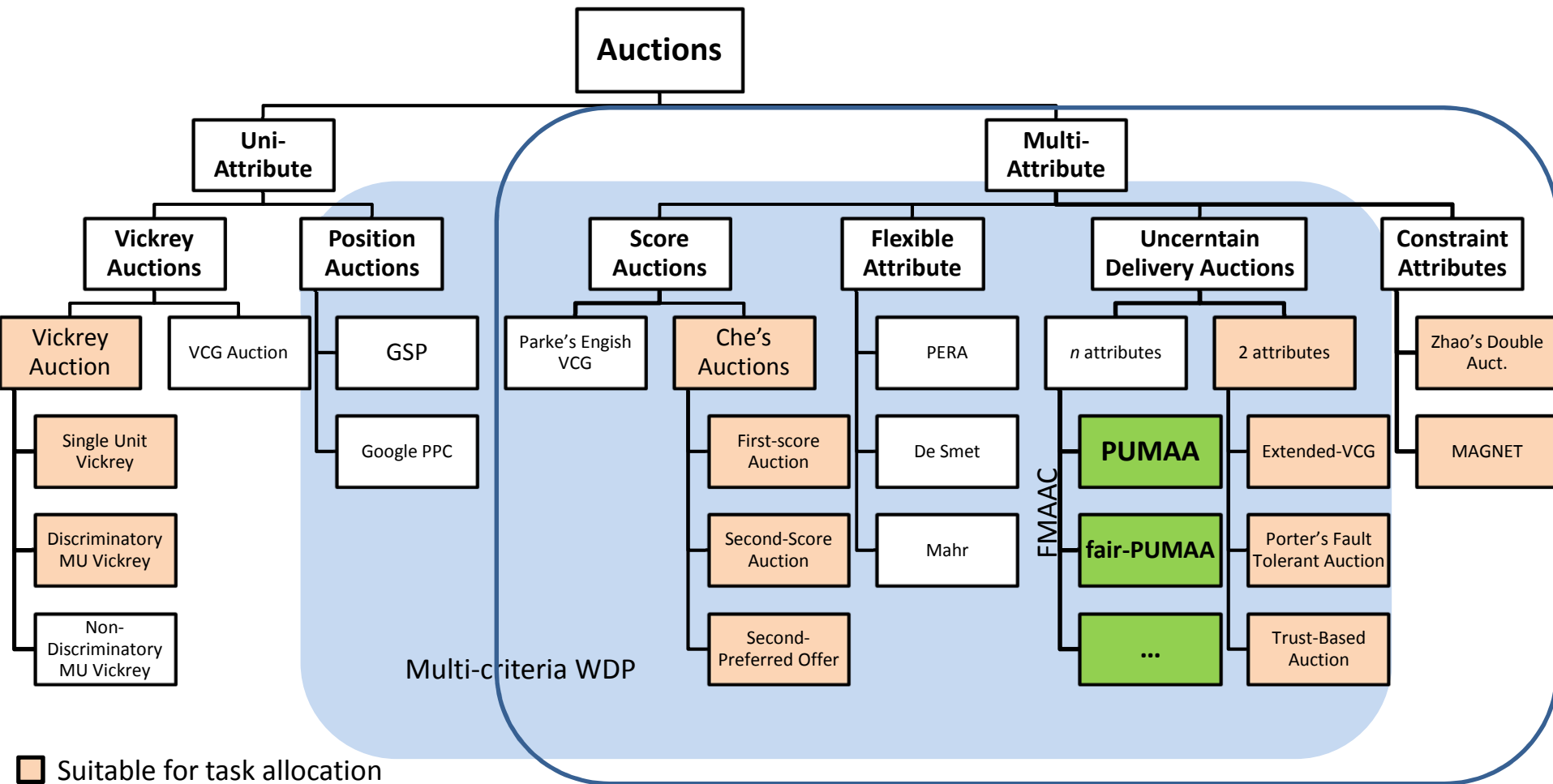
# Auction dimensionality

	Uni-attribute auction	Multi-attribute auction
Uni-criteria WDP	Vickrey Auction Multi-unit Vickrey Auctions VCG Auction Generalized Second Price English Auctions Dutch Auctions	Zhao's Double Auction MAGNET
Multi-criteria WDP	Google PPC Auction	Che's Auctions Parkes Modified VCG David's English Auction PERA De Smet Auction Mahr Auction VCG-POS Porter's Fault Tolerant Auc. Ramchurn's Trust Auc.

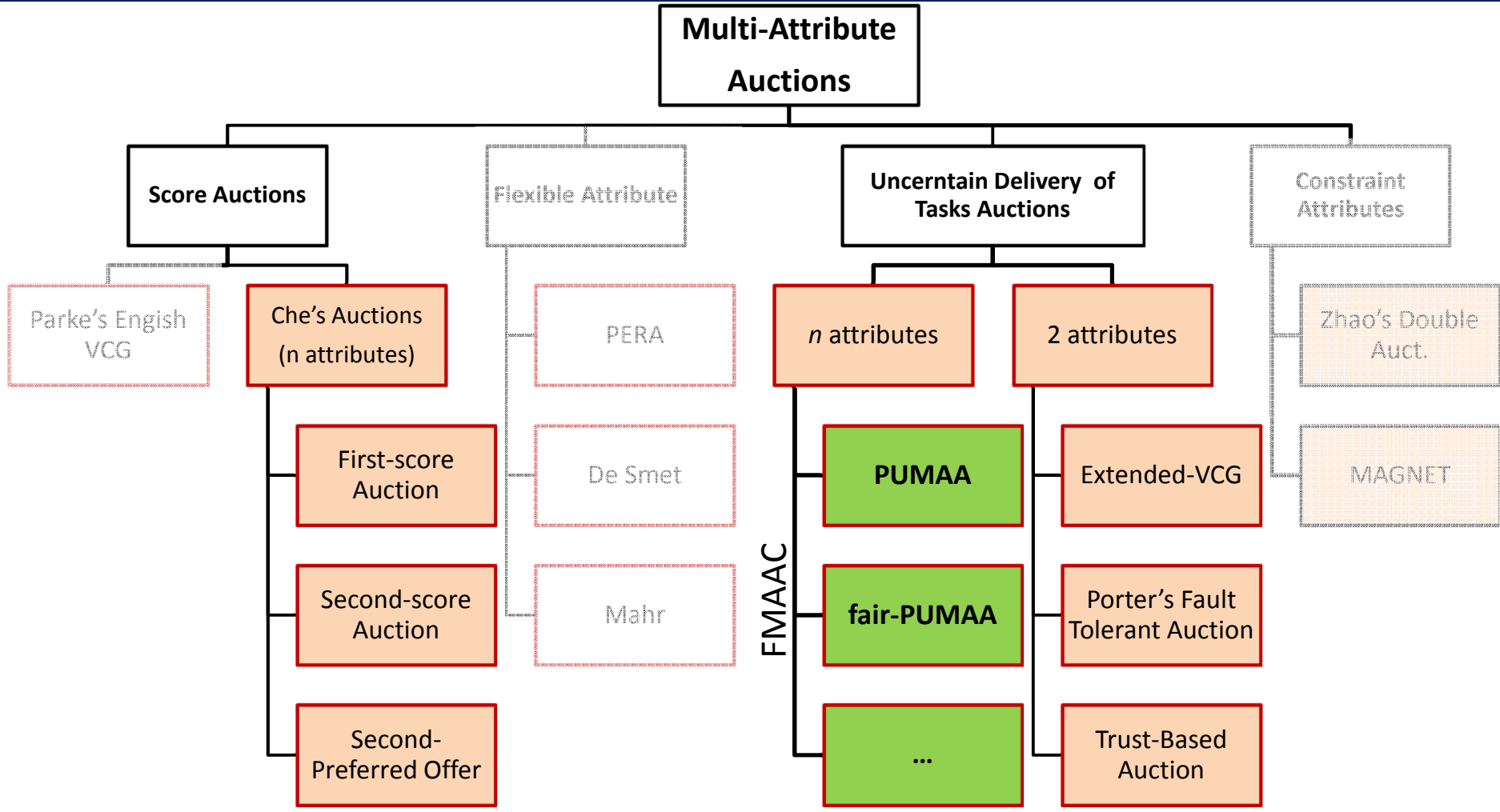




# Multi-attribute resource/task allocation



# Multi-attribute resource/task allocation



Suitable for task allocation
  Multi-criteria WDP



# PUMAA: Preserving Utility Multi-attribute Auctions



# Requirements

- Reverse auction mechanism for task & resource allocation
- Several attributes
- Incentive Compatible
  - Economic cost (bidders bid their real economic aims)
  - Attributes (bidders submit the attributes they intend to deliver)
- Tolerance to uncertainty of task delivery
  - The delivered attributes may vary from the ones agreed
- Robustness (avoid utility loss)

[2] *Multi-Attribute Auction Mechanism for Supporting Resource Allocation in Business Process Enactment*. A Pla, B López, J Murillo STAIRS@ECAI 2012, 228-239



# Assumptions & limitations

- Unknown task schedule (allocated on-the-go)
  - Discards COP solvers, genetic algorithms, etc.
- Tasks are always developed (in better or worst conditions)
- The variation of the task attributes affects agents utilities
- Bidding strategies are out of the thesis scope
- No externalities: Bidders are just concerned in the present auction



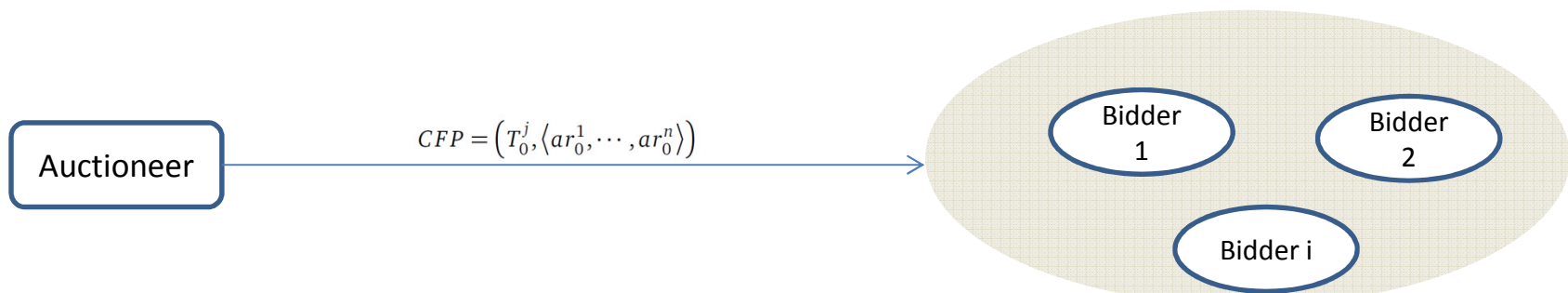
# 1. PUMAA: Call for Proposals

- An auctioneer  $a_0$  needs to allocate a task  $T^j$

$$T^j = \langle pa_1^j, \dots, pa_m^j \rangle$$

- Sends a call for proposals (CFP) to all the bidders
  - Specifies the task
  - Specifies the attribute requirements

$$CFP = \left( T_0^j, \langle ar_0^1, \dots, ar_0^n \rangle \right)$$



## 2. PUMAA: Bidding

- Bidders ( $a_i$ ) evaluates the CFP and submits a bid

$$B_i = (b_i, AT_i)$$

- Utility of a bidder:

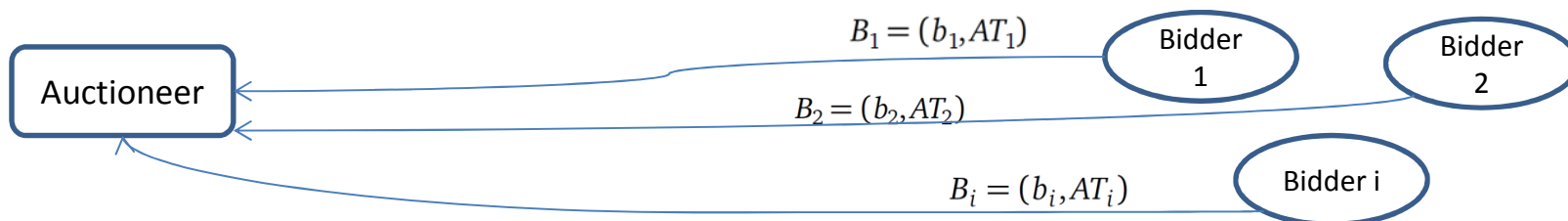
$$b_i^t = v_i(T_0^j, AT_i^t)$$

$$u_i(p_i, b_i^t) = p_i - b_i^t$$

- Truthful or untruthful bid

$$B_i = (b_i, AT_i) | b_i = b_i^t \vee AT_i = AT_i^t$$

$$B_i = (b_i, AT_i) | b_i \neq b_i^t \vee AT_i \neq AT_i^t$$



### 3. PUMAA: Winning determination problem

- The winner is determined by an **evaluation function  $V_0$**

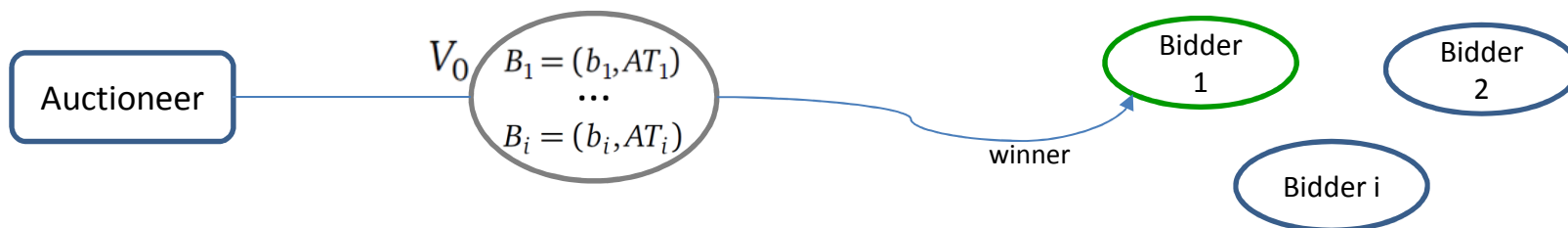
$$V_0(b_i, AT_i)$$

$$argmin_i(V_0(b_i, AT_i))$$

- The evaluation function will maximize the auctioneer  $a_0$ 's expected utility  $\bar{u}$ .

$$\bar{u}_0(T_0^j, b_i, AT_i) = v_0(T_0^j) - f_0(b_i, AT_i)$$

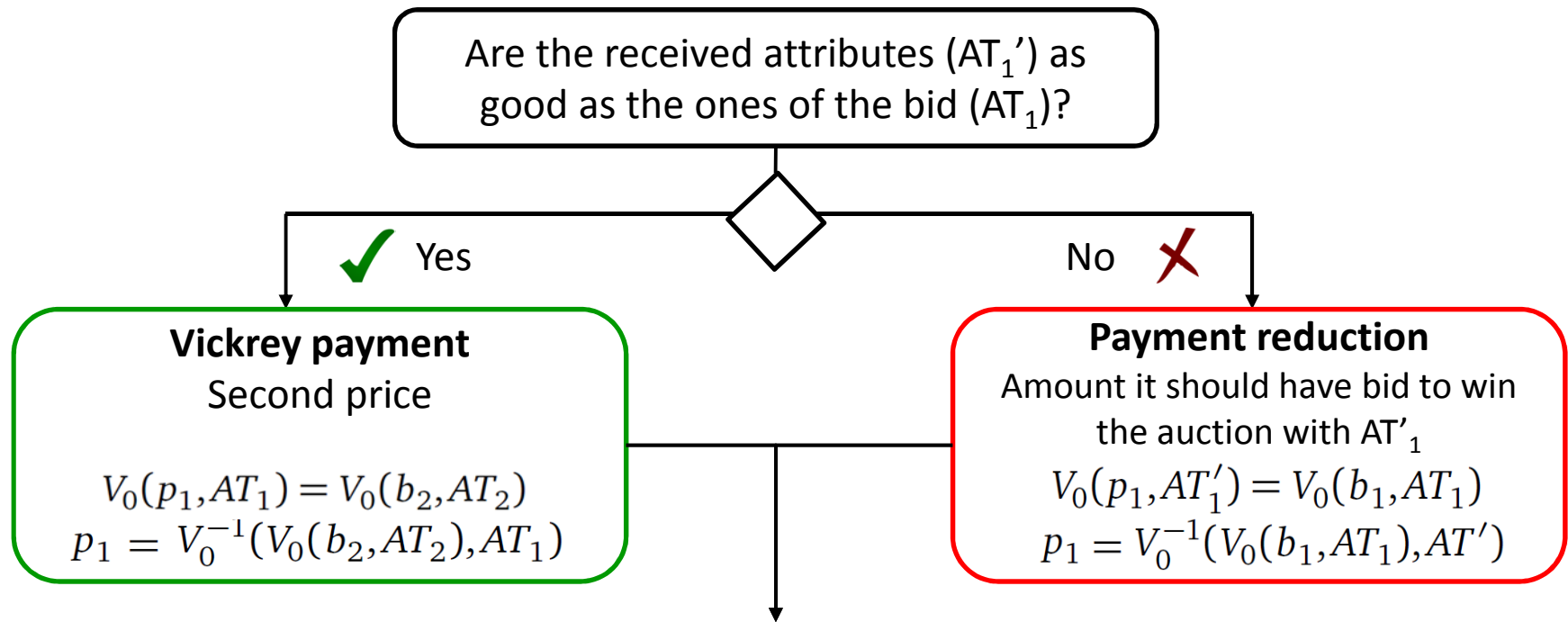
$\swarrow$  Value of the task  
 $\searrow$  valuation of the attributes (e.g.  $V_0$ )





# 4. PUMAA: Payment rule

- Conditional Vickrey-based payment:



$$p_1 = \begin{cases} V_0^{-1}(V_0(b_2, AT_2), AT_1) & \text{if } AT'_1 \succeq AT_1 \\ V_0^{-1}(V_0(b_1, AT_1), AT') & \text{if } AT'_1 \prec AT_1 \end{cases}$$



# Evaluation ( $V_0$ ) function requirements

- Real Valued Function
  - $V_0(b,AT)$  must return a real number evaluation for each bid
    - The payment mechanism involves the numeric evaluation obtained by the second best bid.
  - Discards multi-criteria methods which result in ranked lists or orders without numeric valuations.
    - If there is not a numeric evaluation, the payment cannot be computed

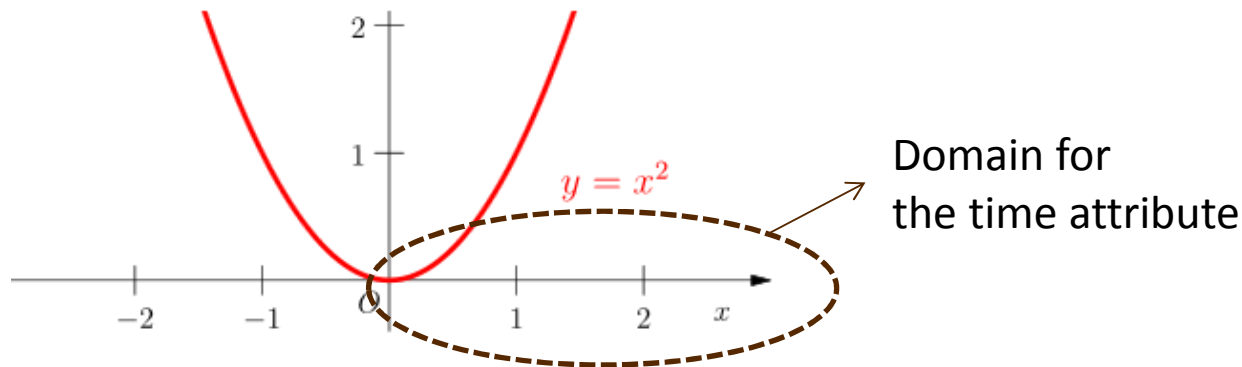
[3] *Multi Criteria Operators for Multi-attribute Auctions* A Pla, B López, J Murillo Modeling Decisions for Artificial Intelligence (MDAI) 2012, 318-328.



# Evaluation function requirements

- Monotonicity

- If an attribute is improved, the score of the evaluation must also improve.
- Ensures that, for every possible value in the attribute domain,  $V_0(b, AT)$  will return a value.
- Only applied in the range of values an attribute can take.
  - Example: If an attribute can only take positive values (time duration), it can be evaluated using its square function.



# Evaluation function requirements

- Bijection

- In order to calculate the payment,  $V_0(b, AT)$  must have a bijective behavior regarding the economic attribute.

- Given:

$$V_0(b, AT) = x$$

its reverse function will be

$$V_0^{-1}(x, AT) = b$$

where  $b$  can be just one value

- Need of distinguish between economic attribute  $b$  and  $AT$

- Avoid vertical asymptotes to avoid payments of infinite value



# Evaluation function examples

- Product

$$V_0(b_i, AT_i) = b_i * \prod_{j=1}^n at_i^j$$

$$p_1 = \begin{cases} \frac{b_2 * \prod_{j=1}^n at_2^j}{\prod_{j=1}^n at_1^j} & \text{if } AT'_1 \succeq AT_1 \\ \frac{b_1 * \prod_{j=1}^n at_1^{j'}}{\prod_{j=1}^n at_1^j} & \text{if } AT'_1 \prec AT_1 \end{cases}$$

- Weighted sum

$$V_0(b_i, AT_i) = \mu_0 b_i + \sum_{j=1}^n \mu_j at_i^j$$

$$p_1 = \begin{cases} \frac{\mu_0 b_2 + \sum_{j=1}^n \mu_j (at_2^j - at_1^j)}{\mu_0} & \text{if } AT_1 \succeq AT'_1 \\ \frac{\mu_0 b_1 + \sum_{j=1}^n \mu_j (at_1^{j'} - at_1^j)}{\mu_0} & \text{if } AT_1 \prec AT'_1 \end{cases}$$

- Mathematical norms

- E.g. Euclidean norm

$$V_0(b_i, AT_i) = \sqrt{b_i^2 + \sum_{j=1}^n (at_i^j)^2}$$

$$p_1 = \begin{cases} \sqrt{\frac{b_2^2 + \sum_{j=1}^n ((at_2^j)^2 - (at_1^j)^2)}{b_1^2 + \sum_{j=1}^n ((at_1^{j'})^2 - (at_1^j)^2)}} & \text{if } AT'_1 \succeq AT_1 \\ \sqrt{\frac{b_2^2 + \sum_{j=1}^n ((at_2^j)^2 - (at_1^j)^2)}{b_1^2 + \sum_{j=1}^n ((at_1^{j'})^2 - (at_1^j)^2)}} & \text{if } AT'_1 \prec AT_1 \end{cases}$$

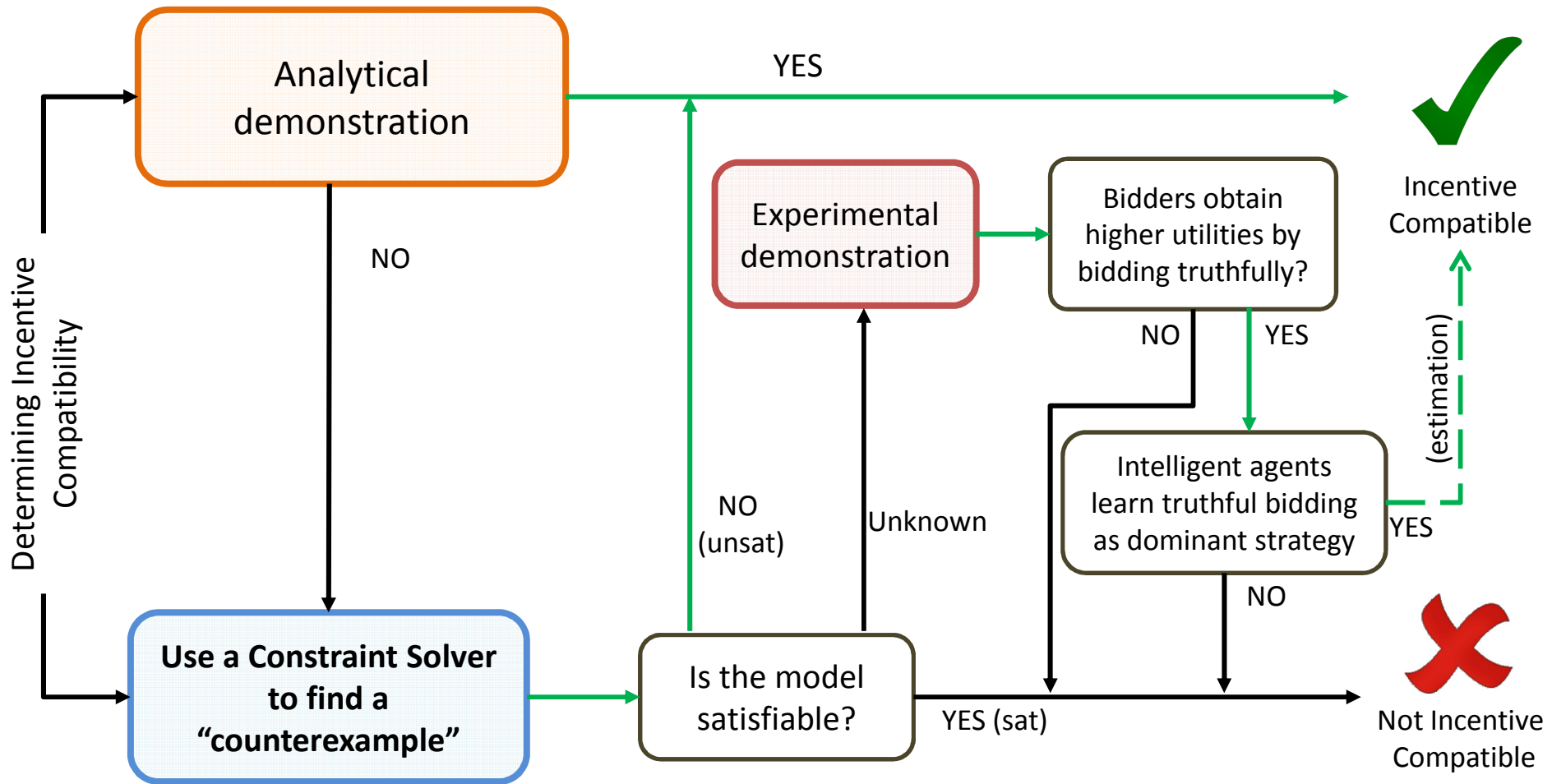
- Weighted sum of functions

$$V_0(b_i, AT_i) = \mu_0 g_0(b_i) + \sum_{j=1}^n \mu_j g_j(at_i^j)$$

$$p_1 = \begin{cases} \frac{g'_0(\mu_0 g_0(b_2) + \sum_{j=1}^n (\mu_j g_j(at_2^j) - \mu_j g_j(at_1^j)))}{\mu_0} & \text{if } AT'_1 \succeq AT_1 \\ \frac{g'_0(\mu_0 g_0(b_1) + \sum_{j=1}^n (\mu_j g_j(at_1^{j'}) - \mu_j g_j(at_1^j)))}{\mu_0} & \text{if } AT'_1 \prec AT_1 \end{cases}$$



# PUMAA: Incentive compatibility



# PUMAA: Incentive compatibility

- Finding a counter example with a constraint solver
  - Incentive compatible: For any feasible bid, the bidder’s utility is higher by submitting the truthful attribute information:

$$\forall i \in \mathbb{N}, \forall (b_i, b_i^t, AT_i, AT_i^t) \in \mathbb{R} > 0 : \{(u_i(b_i, AT_i, p) \leq u_i(b_i^t, AT_i^t, p')) | (b_i^t \neq b_i) \vee (AT_i^t \neq AT_i)\}$$

- ¿Is there any case not fulfilling this condition?
- Modeling the mechanism using an inequation system.
- Modeling the case where lying is better.
- If the inequation system is solvable → **NOT INCENTIVE COMPATIBLE**
- If the inequation system has no solution → **INCENTIVE COMPATIBLE**

[4] *How to Demonstrate Incentive Compatibility in Multi-Attribute Auctions* A Pla, B López, J Murillo Congrès Català d'Intel·ligència artificial (CCIA) 2013 FAIA 256, 303-306



# PUMAA: Incentive compatibility

- Inequation system for the weighted sum





$$\left. \begin{aligned}
 & \text{(a)} \quad a(AT_1) \neq a(AT'_1) \vee b_1 \neq b'_1 \\
 & \text{(b)} \quad \mu_1 b_1 + \mu_2 a(AT_1) < \mu_1 b_2 + \mu_2 a(AT_2) \\
 & \text{(c)} \quad \text{win} = \begin{cases} 1 & \text{if } (\mu_1 b_2 + \mu_2 a(AT_2)) > \mu_1 b_1^t + \mu_2 a(AT'_1) \\ 0 & \text{otherwise} \end{cases} \\
 & \text{(d)} \quad \text{win} \left( \frac{\mu_1 b_2 + \mu_2 a(AT_2) - \mu_2 a(AT'_1)}{\mu_1} - b_1^t \right) < \left( \frac{\mu_1 b_1 + \mu_2 a(AT_1) - \mu_2 a(AT'_1)}{\mu_1} - b_1^t \right) \\
 & \text{(e)} \quad \mu_1 + \mu_2 = 1 \\
 & \text{(f)} \quad 0 < \mu_1 < 1 \\
 & \text{(g)} \quad 0 < \mu_2 < 1
 \end{aligned} \right\}$$

- Using Z3 constraint solver (real arithmetic logic):  
 Not solvable → **Incentive Compatible**



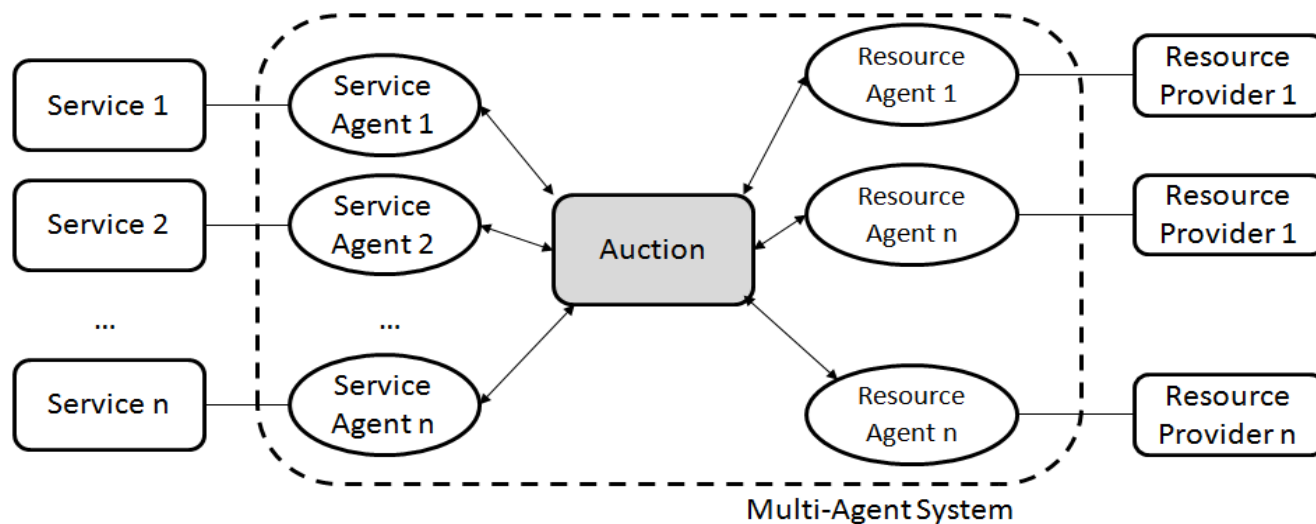


# PUMAA: Other properties

- Efficiency 
- Buyer optimality 
- Budget-balance 
- Social welfare Utilitarian
- Robustness Reduce utility loss
- Reliability 



# PUMAA Results – Simulation environment



- Real data-based multi-agent system simulation
- Service agent
  - Requires resource with specific skills
  - Different priority / deadline
  - Probability of occurrence
- Resource provider agent
  - Requires resource with specific skills
  - Different execution time per task
  - Bidding strategy:
    - Honest, adaptive or cheating

[5] Petri net-based process monitoring: A workflow management system for process modelling and monitoring, A Pla, P Gay, J Meléndez, B López Journal of Intelligent Manufacturing, 2012 1-16

# PUMAA Results: Experiments

Experiment	Goal	Scenarios	Methods evaluated	Metrics
1	<b>Uni-attribute vs multi-attribute</b>	Synthetic data Real data	<ol style="list-style-type: none"> <li>1. First price</li> <li>2. Fastest resource</li> <li>3. Vickrey MA</li> <li>4. PUMAA</li> </ol>	<ul style="list-style-type: none"> <li>• Task allocation cost</li> <li>• Delays produced</li> </ul>
2	Strategy proofness	Synthetic data Real data Reinforcement Learning	<ol style="list-style-type: none"> <li>1. PUMAA Different bidding strategies</li> </ol>	<ul style="list-style-type: none"> <li>• Bidders utility</li> <li>• Auctioneers utility</li> <li>• Dominant strategies</li> </ul>
3	Evaluation function influence	Product Weighted sum Euclidean norm	<ol style="list-style-type: none"> <li>1. PUMAA different evaluation functions</li> </ol>	<ul style="list-style-type: none"> <li>• Auctioneer's utility</li> <li>• Bidder's utility</li> <li>• Type of allocation</li> </ul>
4	<b>Utility preservation and robustness to cheaters</b>	Ascendant number of cheaters	<ol style="list-style-type: none"> <li>1. PUMAA</li> <li>2. Che's SP</li> </ol>	<ul style="list-style-type: none"> <li>• Auctioneer's utility</li> <li>• Service cost</li> <li>• Delays produced</li> </ul>

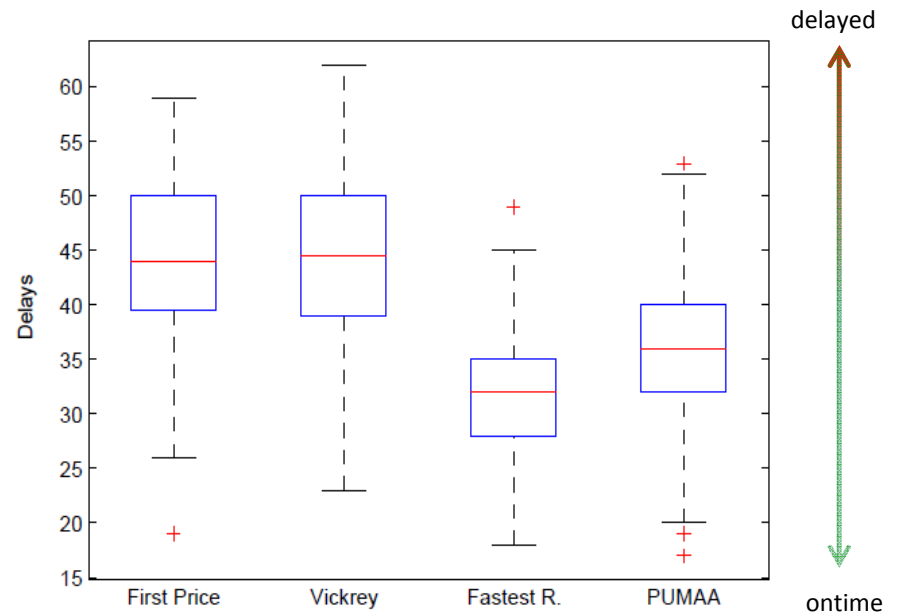
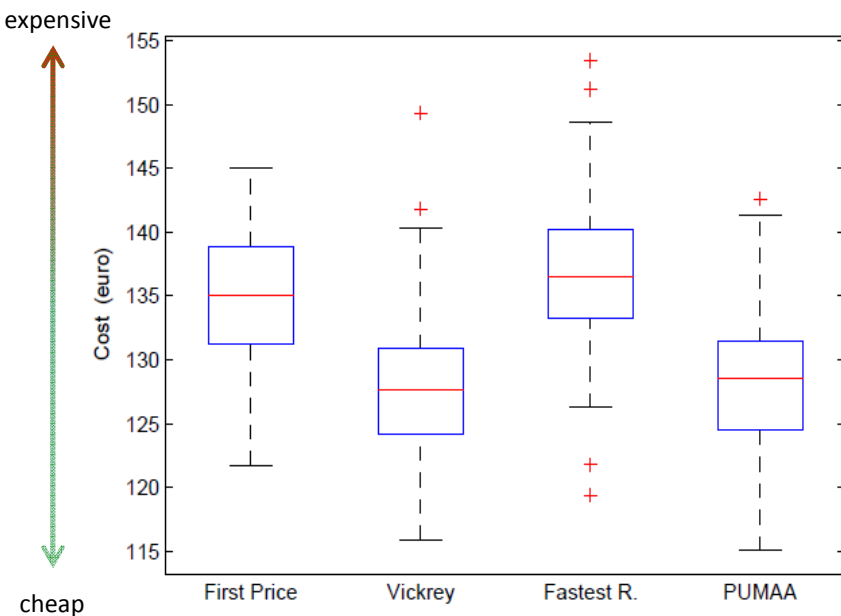
[2] *Multi-Attribute Auction Mechanism for Supporting Resource Allocation in Business Process Enactment*. A Pla, B López, J Murillo STAIRS@ECAI, Montpellier 2012, 228-239

[6] *Workflow resource allocation through auctions* A Pla, B López, J Murillo Artificial Intelligence and Logistics (AILOG@IJCAI), Barcelona 2011, 55



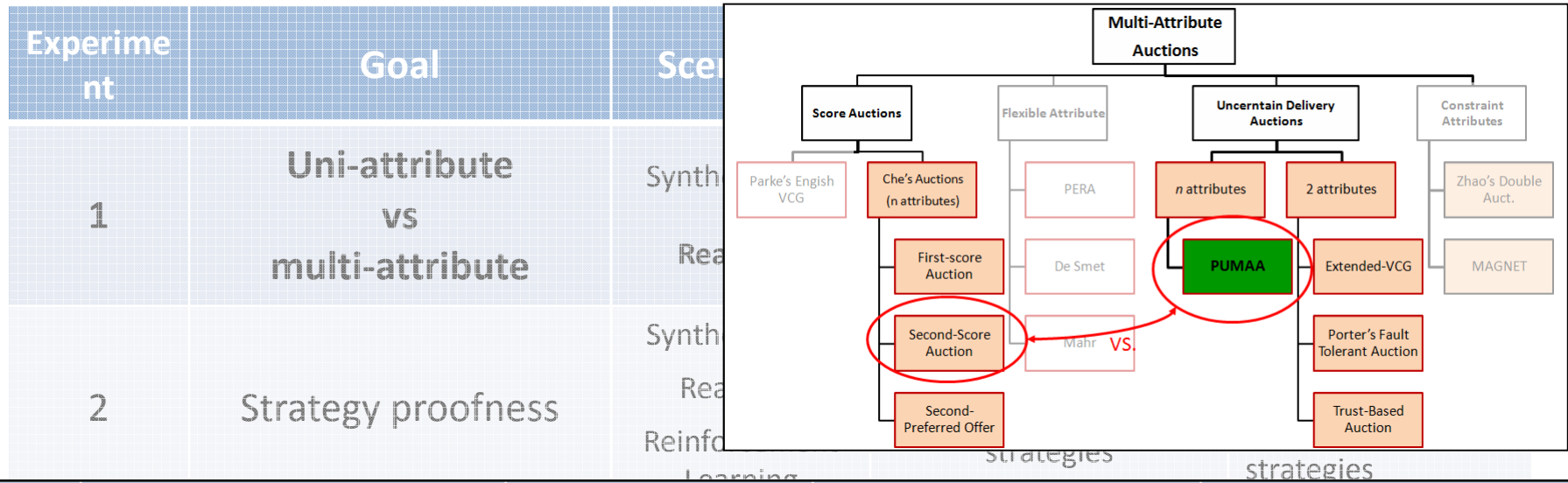
# PUMAA Results: Uni-attribute vs. Multi-attribute

- Service cost allocation cost
- Delays produced



- PUMAA obtains the best balance between attributes: low cost / few delays

# PUMAA Results: Experiments

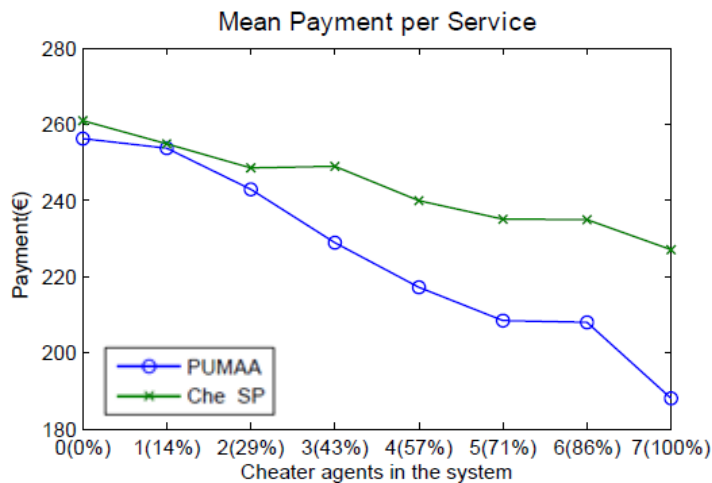
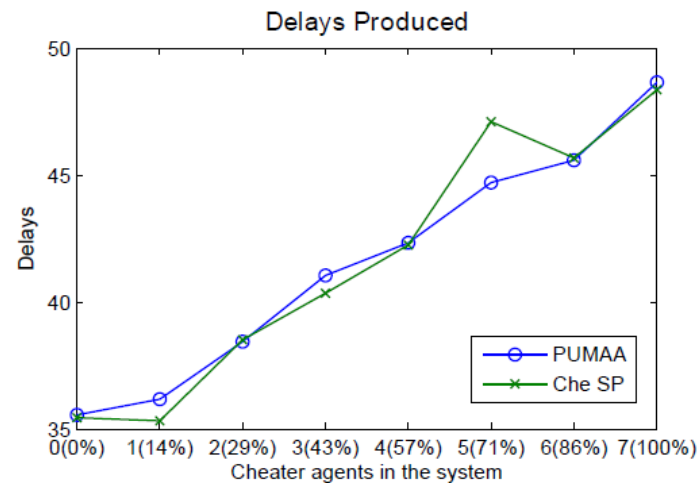
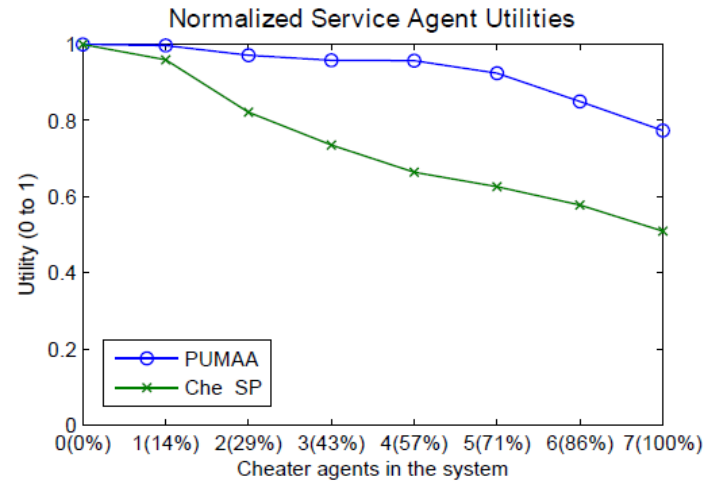
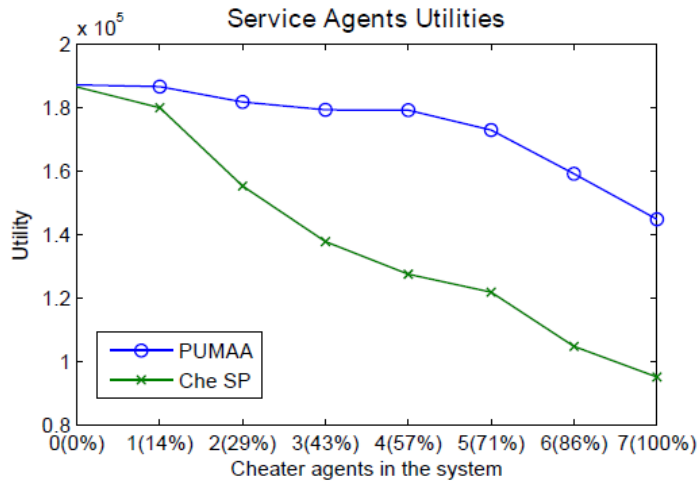


4	<b>Utility preservation and robustness to cheaters</b>	<b>Ascendent number of cheaters</b>  [0 cheaters, 1 cheater, ... , all cheaters]	1. PUMAA  2. Che's Second price	<ul style="list-style-type: none"> <li>• Auctioneer's utility</li> <li>• Service costs</li> <li>• Delays produced</li> </ul>
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[2] Multi-Attribute Auction Mechanism for Supporting Resource Allocation in Business Process Enactment. A Pla, B López, J Murillo STAIRS@ECAI, Montpellier 2012, 228-239  
 [6] Workflow resource allocation through auctions A Pla, B López, J Murillo Artificial Intelligence and Logistics (AILOG@IJCAI), Barcelona 2011, 55



# PUMAA – Results: Utility preservation



# FMAAC: Framework for Multi-attribute Auction Customization



# Framework for Multi-attribute Auction Customization

- Study the types of attributes which can appear in a multi-attribute auction
- Using such study, design a framework for customizing multi-attribute auctions





# Attribute typologies in multi-attribute auctions

- Study the kind of attributes appearing in different auctions:
  - GSP, Vickrey, Porter’s auction, Che’s auctions, etc.
  
- Ownership
  - Who is introducing the attribute into the auction
  - **Bidder-provided** or **auctioneer-provided**
  
- Verifiability
  - Can the auctioneer check the veracity of the attribute
  - **Verifiable** or **unverifiable**



# Unverifiable bidder-provided attributes

	Verifiable	Unverifiable
Bidder Ownership	<p><b>Verifiable bidder provided attributes</b></p> <p>Delivery times, qualities, energy consumptions, CO<sub>2</sub> emissions...</p>	<p><b>Unverifiable bidder provided attributes</b></p> <p>Economic cost, CO<sub>2</sub> emission quota</p>
Auctioneer Ownership	<p><b>Auctioneer provided attributes</b></p>	
	<p>Auctions won, past performance ...</p>	<p>Agent's reputation</p>

- Unverifiable bidder-provided attrs.
  - Real value only known by the bidder
  - True-value not known by auctioneer
  - Currency of the auction
  - Appear in all auctions
  - Only 1 attribute



# Verifiable bidder-provided attributes

	Verifiable	Unverifiable
Bidder Ownership	<p><b>Verifiable bidder provided attributes</b></p> <p>Delivery times, qualities, energy consumptions, CO<sub>2</sub> emissions...</p>	<p><b>Unverifiable bidder provided attributes</b></p> <p>Economic cost, CO<sub>2</sub> emission quota</p>
Auctioneer Ownership	<p><b>Auctioneer provided attributes</b></p> <p>Auctions won, past performance ...</p>	
		<p>Agent's reputation</p>

- Verifiable bidder-provided attr.
  - The auctioneer can check if the attribute is truthful
  - Checking before payment
  - Appear only in multi-attribute auctions
  - *n* attributes



# Auctioneer-provided attributes

	Verifiable	Unverifiable
Bidder Ownership	<p><b>Verifiable bidder provided attributes</b></p> <p>Delivery times, qualities, energy consumptions, CO<sub>2</sub> emissions...</p>	<p><b>Unverifiable bidder provided attributes</b></p> <p>Economic cost, CO<sub>2</sub> emission quota</p>
Auctioneer Ownership	<p><b>Auctioneer provided attributes</b></p> <p>Auctions won, past performance ...</p>	
		<p>Agent's reputation</p>

- Auctioneer-provided attrs.
  - Introduced by the auctioneer
  - Describe auctioneer's beliefs and information regarding past auctions
  - Uni and multi-attribute auctions
  - *n attributes*
  - Multi-attribute auctions



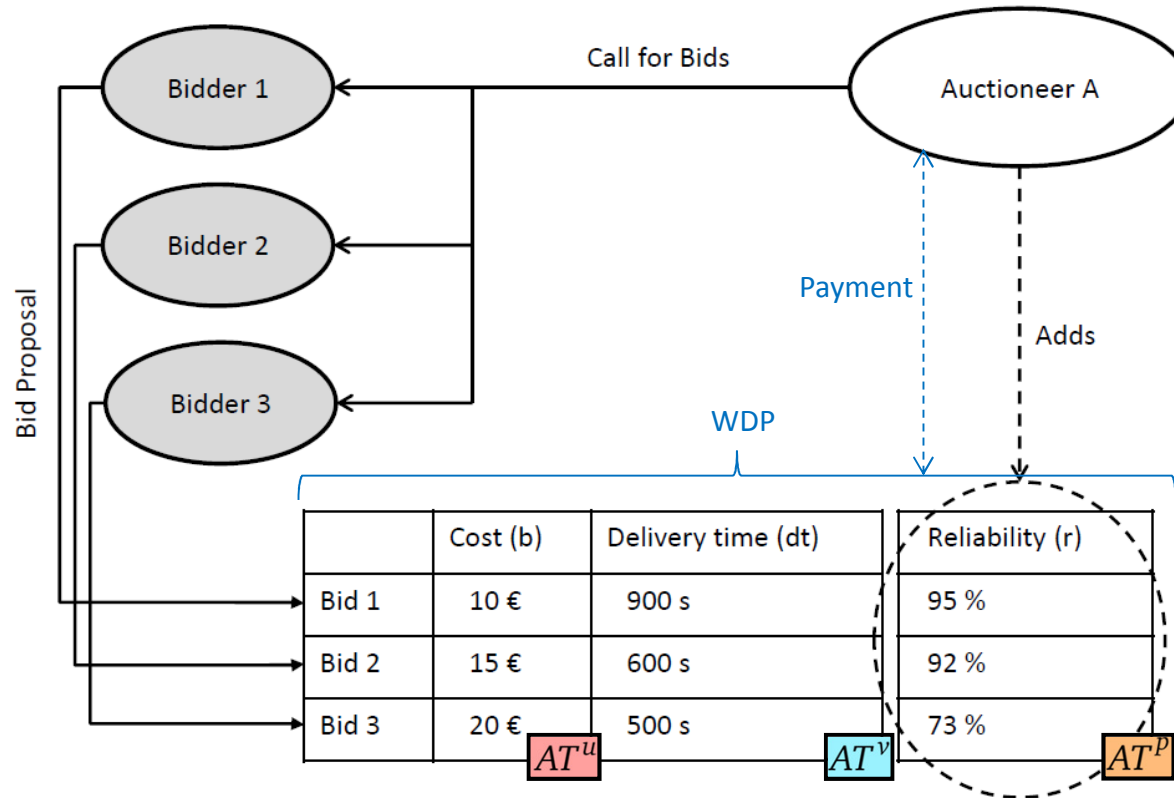
# FMAAC

- Framework for **Multi-Attribute Auction Customization**
- Generalizes PUMAA to include auctioneer-provided attributes
- Allow mechanism designers to cover new problems using information collected in recurrent auctions:
  - Egalitarian allocations
  - Reliable allocations

[7] *Multi-Attribute Auctions with Different Types of Attributes: Enacting Properties in Multi-Attribute Auctions*, A Pla, B López, J Murillo, N Maudet *Expert Systems with Applications* 41(10), 2014, 4829-4843



# FMAAC



- Steps of FMAAC:
  1. Call for proposals
  2. Bidding
  3. Winner determination
  4. Payment
  5. Attribute information process

[7] Multi-Attribute Auctions with Different Types of Attributes: Enacting Properties in Multi-Attribute Auctions, A Pla, B López, J Murillo, N Maudet Expert Systems with Applications 41(10), 2014, 4829-4843



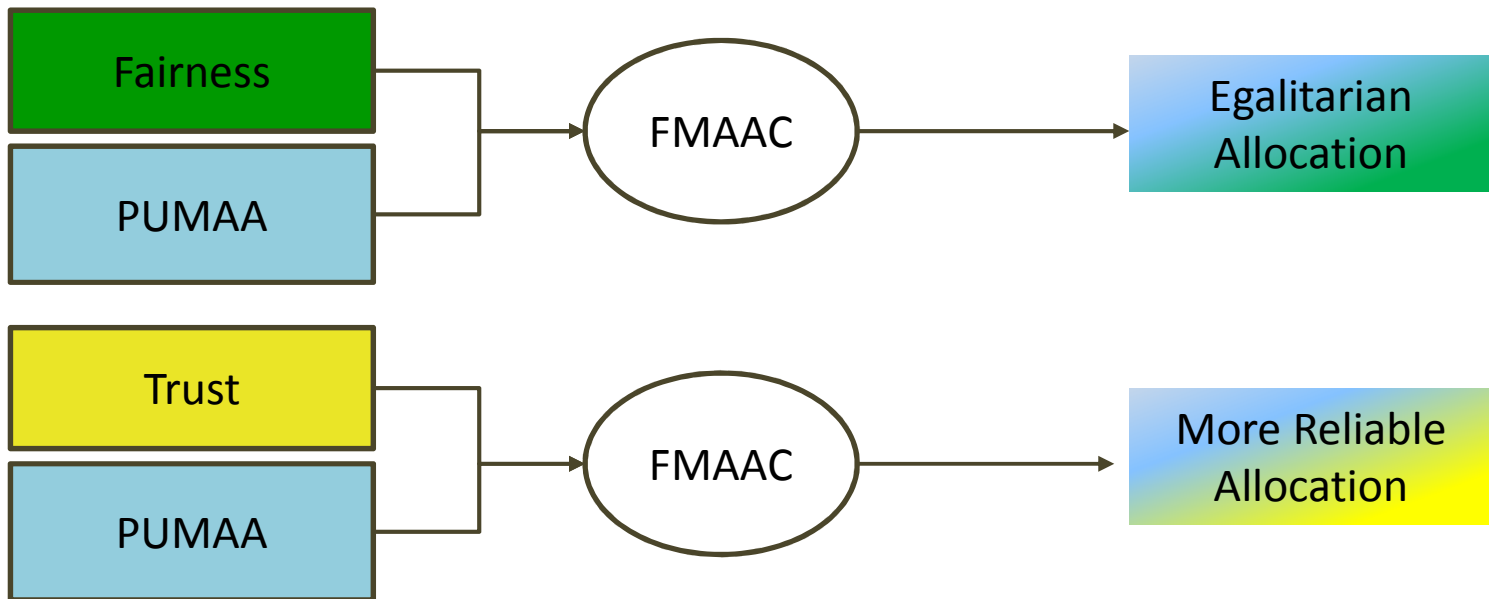
# FMAAC: Steps

	PUMAA	FMAAC
CFP	proposes: $AT^v$	=
Bidding	bid submission: $AT^u AT^v$	=
WDP	bid evaluation: $V_0( AT^u AT^v )$	Bid structure: $AT^u AT^v + AT^p$ Bid evaluation $V_0( AT^u AT^v AT^p )$
Payment Rule	compute payment using: $AT^u$ $AT^v$	compute payment using: $AT^u$ $AT^v$ $AT^p$
Attribute Information Update	-	Collects information of the auction: $Update( AT^p )$



# Auctioneer provided attributes in FMAAC

- Auctioneer provided attributes will modify multi-attribute auction allocation





# Multi-dimensional Fairness for Multi-attribute Resource Allocation



# Challenges vs. Contributions

- Multi-attribute IC

- Workflow related issues

- Recurrent auctions' issues

- PUMAA

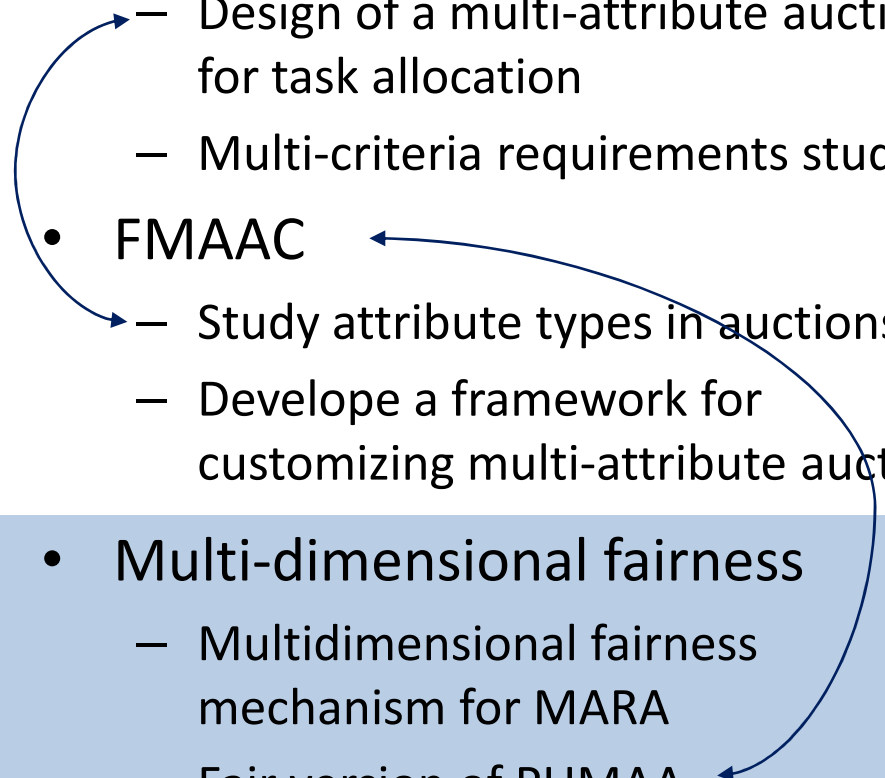
- Design of a multi-attribute auction for task allocation
- Multi-criteria requirements study

- FMAAC

- Study attribute types in auctions
- Develop a framework for customizing multi-attribute auctions

- Multi-dimensional fairness

- Multidimensional fairness mechanism for MARA
- Fair version of PUMAA
- Minimize the bidder drop problem



# Multi-dimensional fairness

- Existing fairness methods are **uni-dimensional**.
- **Multi-dimensional** fairness: take into account all bidder-provided attributes.
  - Keep track of the auction victories and results
- Use a priority auctioneer-provided attribute  $w_i$  according to the bidders' auction history:
  - A high  $w_i$  means the agent might leave the market soon.
  - $w_i$  should consider all the attributes
  - $w_i \in [0,1]$

[8] *Multidimensional Fairness for Auction-based Resource Allocation*. A. Pla, B. López, J. Murillo Knowledge-based Systems. (Submitted on November, 2013).



# Quantitative methods

- Based on the number of victories or defeats.
- Won auction coefficient (WOC)
  - Relation between auctions won and auctions participated.
  - Proportional measure.
- Loosing streak (LS)
  - Number of consecutives defeats
  - Include cognitive distortions such as “bad luck sense”
  - Defines a maximum loosing streak in which the player will not increase its priority.

$$w_i = 1 - \frac{1 + \text{won}(a_i)}{1 + \text{par}(a_i)}$$

$$w_i = 1 - \frac{\max(0, ml - ls(a_i))}{ml}$$



# Qualitative methods

- Evaluating the quality of a bid respect to the winner bid:
  - Avoids dummy bids to increase quality
  - Favors high-quality bidders
  - Fitness function to evaluate the bids:

$$q_i = \frac{V_0(B'_i)}{V_0(B'_1)}$$

- Bid-based WOC
  - Relation between the auctions won and the bid quality.

$$w_i = 1 - \frac{1 + \text{won}(a_i)}{1 + \sum_{j=0}^{c-1} q_i^j}$$

- Bid-based LS
  - Quality of the bids during the losing streak.

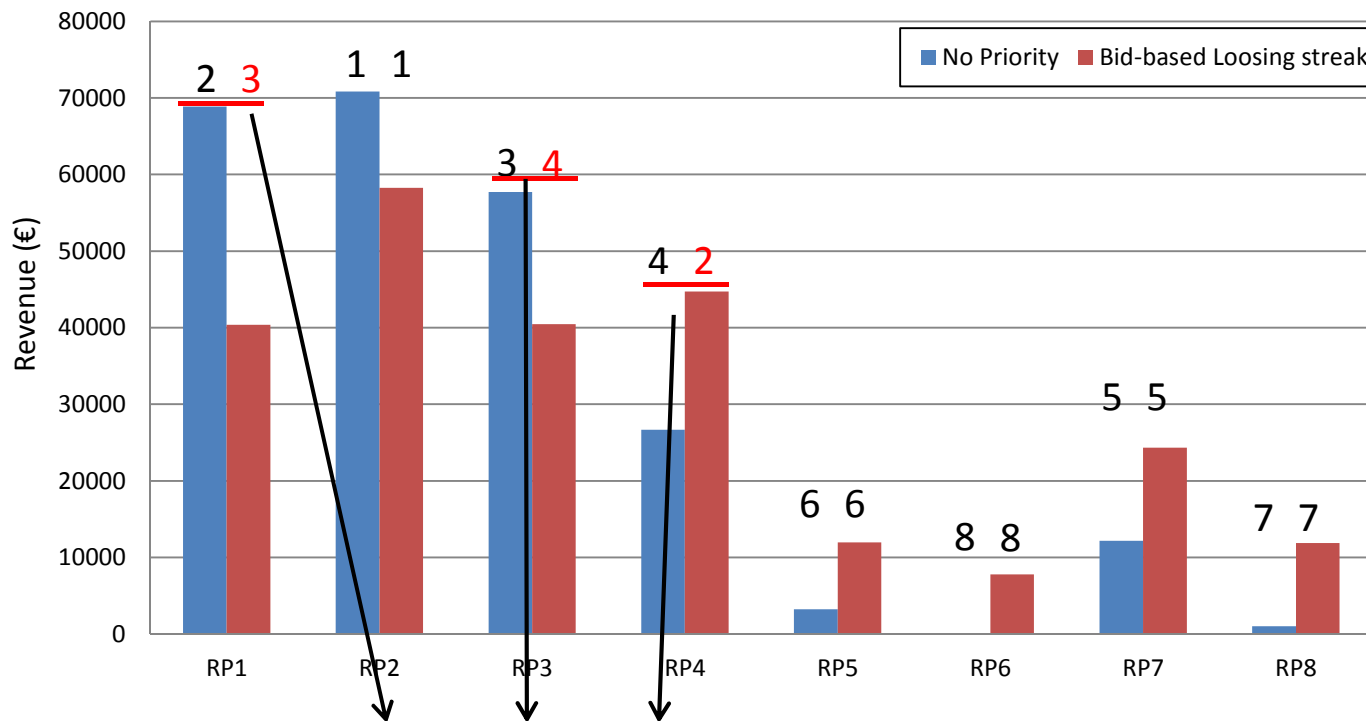
$$w_i = 1 - \frac{\max(0, ml - \sum_{j=c-ls(a_i)}^{c-1} q_i^j)}{ml}$$



# Probabilistic methods

- Priorities can affect the wealth rank of resource providers

**Resource Providers Revenue / Wealth Rank Order**

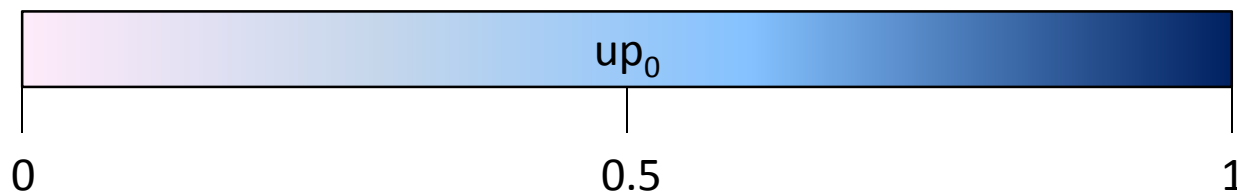


Wealth Rank Disorder Problem



# Probabilistic methods

- Probabilistic version of the previous methods
  - $w_i$  is only update at certain auctions according to an update probability  $up_0$
  - $up_0$  will condition the influence of the priority
  - Reduce the chances of a bidder learning its own priority



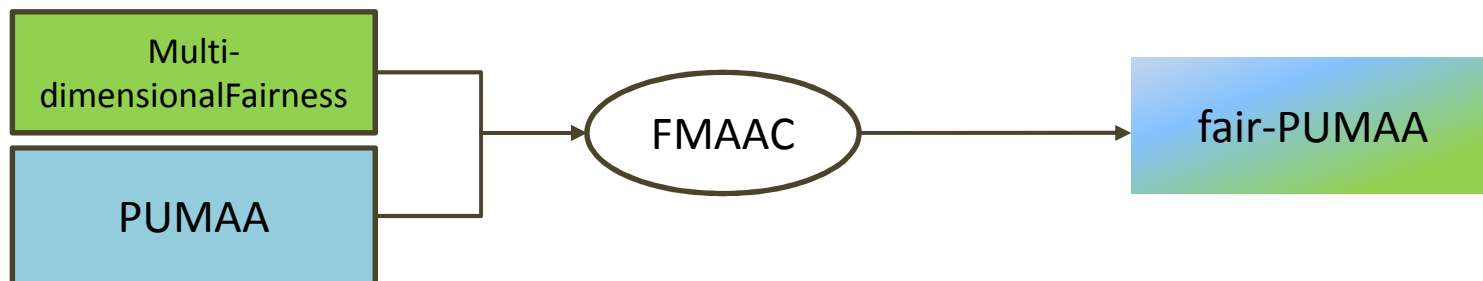
- Priority never updated
- Equivalent to not using priorities

- Priority always updated
- Equivalent to the previous methods

- prob-WOC      • prob-BBWOC      • prob-LS      • prob-BBLS



# fair-PUMAA properties



	PUMAA	fair-PUMAA
Incentive-compatibility	✓	✓ (single auction)
Efficiency	✓	✓ (long run)
Buyer optimality	✗	✗
Budget-balance	✓	✓
Social welfare	Utilitarian	Egalitarian
Robustness	✓	✓
Reliability	≈	≈





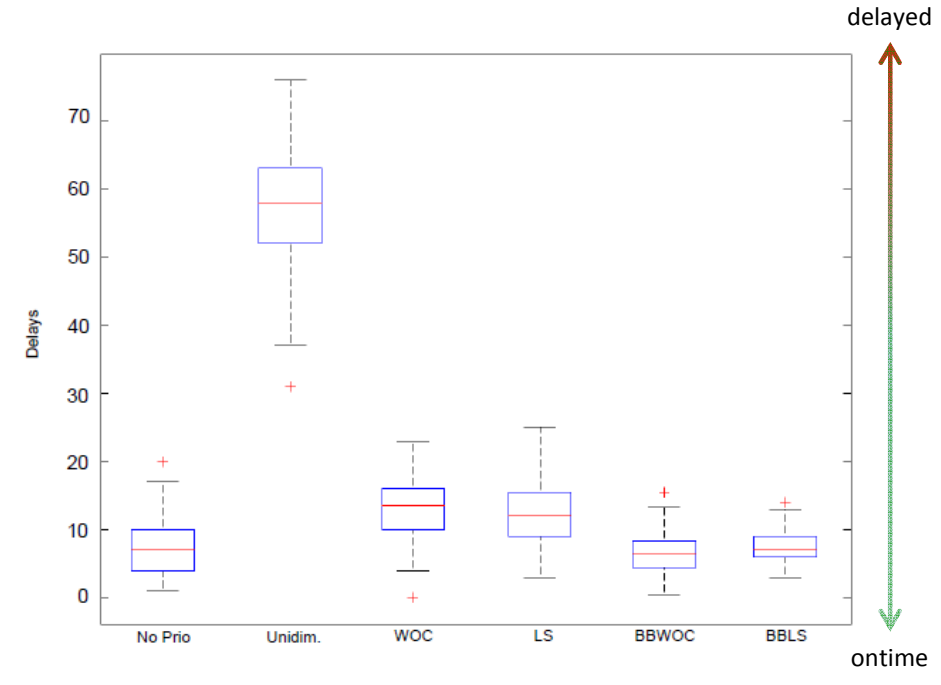
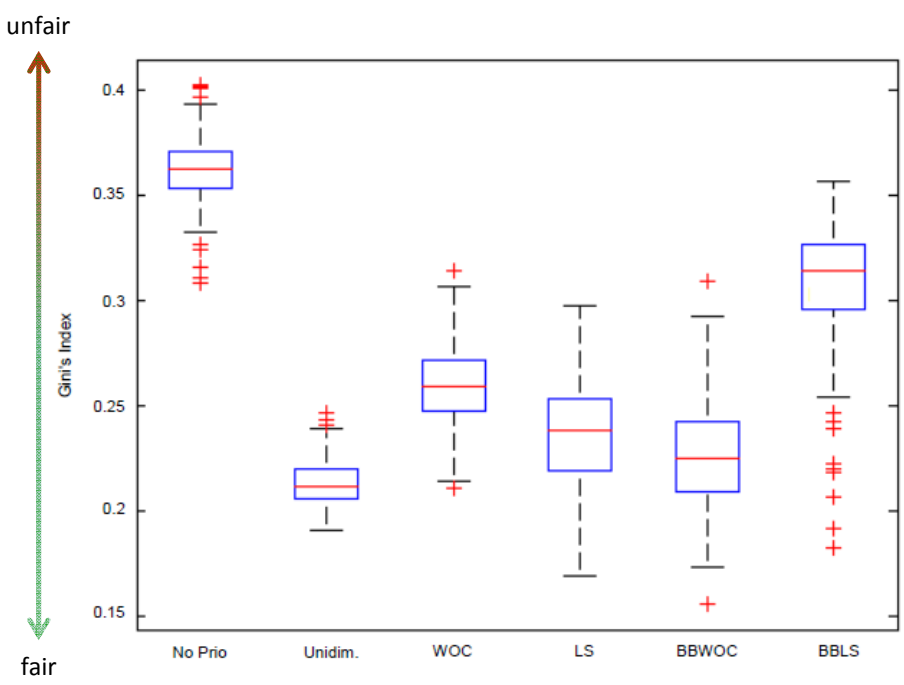
# fair-PUMAA Results: Experiments

Experiment	Goal	Scenarios	Methods evaluated	Metrics
1	Uni-dimensional vs Multi-dimensional	Real data	<ol style="list-style-type: none"> <li>PUMAA</li> <li>Uni-dimensional priority</li> <li>fair-Pumaa</li> </ol>	<ul style="list-style-type: none"> <li>Incomes</li> <li>Expenses</li> <li>Fairness (Gini's)</li> <li>Delays</li> </ul>
2	Probabilistic Methods	Stochastic Methods	<ol style="list-style-type: none"> <li>PUMAA                             <ul style="list-style-type: none"> <li>- probWOC</li> <li>- probLS</li> <li>- probBBWOC</li> <li>- probBBLs</li> </ul> </li> </ol>	<ul style="list-style-type: none"> <li>Wealth Rank Disorder (Spearman's footrule)</li> <li>Fairness (Gini's)</li> </ul>
3	Bidder Drop Problem	Real Data	<ol style="list-style-type: none"> <li>PUMAA</li> <li>fair-PUMAA                             <ul style="list-style-type: none"> <li>- WOC</li> <li>- LS</li> <li>- BBWOC</li> <li>- BBLs</li> <li>- probBWOC</li> </ul> </li> </ol>	<ul style="list-style-type: none"> <li>Active bidders</li> <li>Mean task cost</li> </ul>



# fair-PUMAA results – Uni-dim. vs Multi-dim.

- Gini's index for the resource providers income's
- Delays per simulation



# fair-PUMAA Results: Experiments

50 Resource providers with the same skills:

- 25 follow honest bidding  
 Leave the market if after 50 auctions they don't have benefits
- 25 follow oligopolistic strategy  
 Start working under cost to kick out competence  
 Try to rise the market prices  
 Leave the market if after 100 auctions they don't have benefits

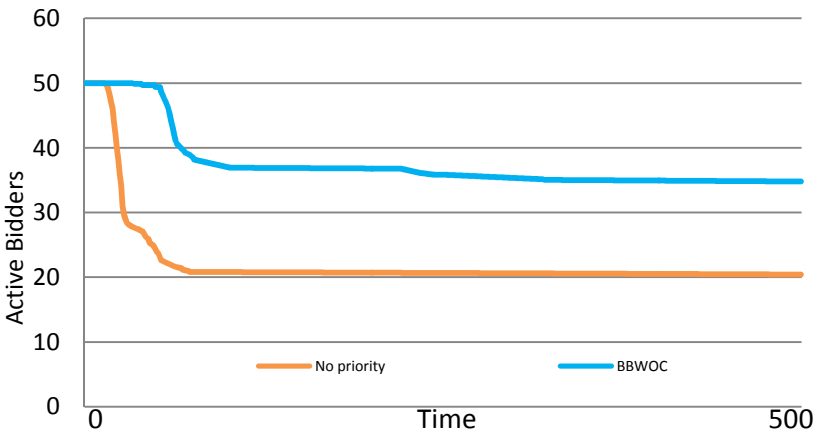
3	<b>Bidder Drop Problem</b>	<b>Real data based</b>	<ol style="list-style-type: none"> <li>1. PUMAA</li> <li>2. fair-PUMAA                     <ul style="list-style-type: none"> <li>• WOC</li> <li>• LS</li> <li>• BBWOC</li> <li>• BBLS</li> <li>• probBWOC</li> </ul> </li> </ol>	<ul style="list-style-type: none"> <li>• Active bidders</li> <li>• Mean task cost</li> </ul>
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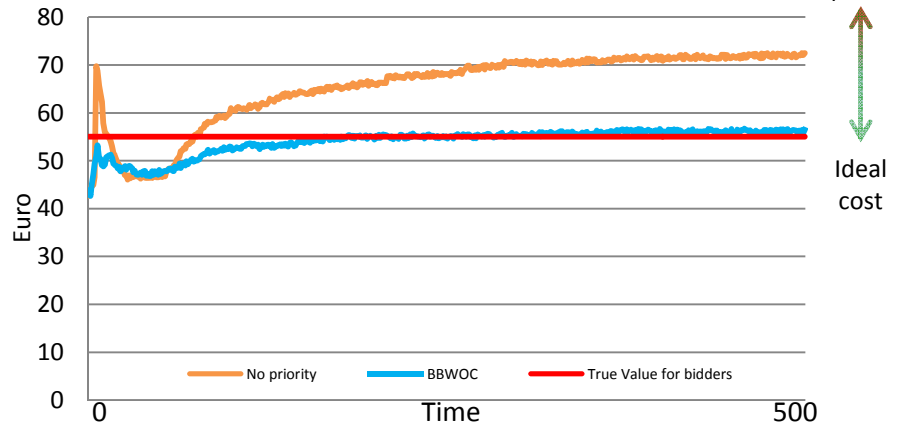
# fair-PUMAA results – Bidder Drop Problem

All agents  
↑  
↓  
Empty market

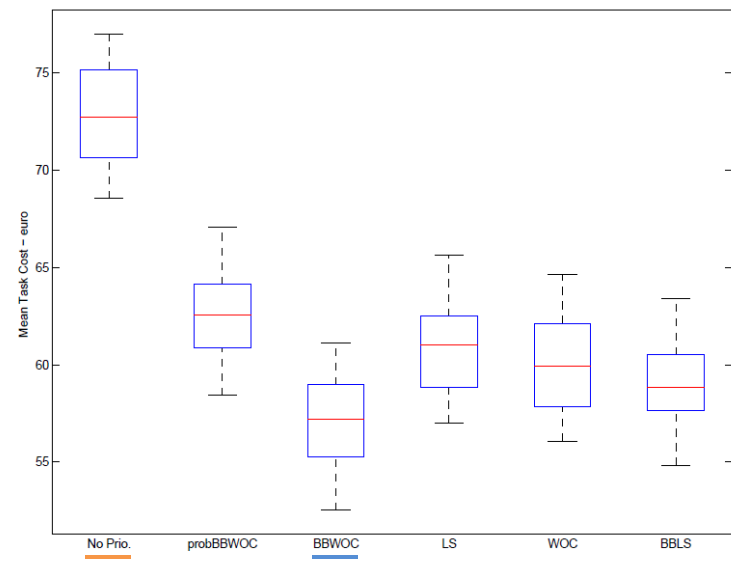
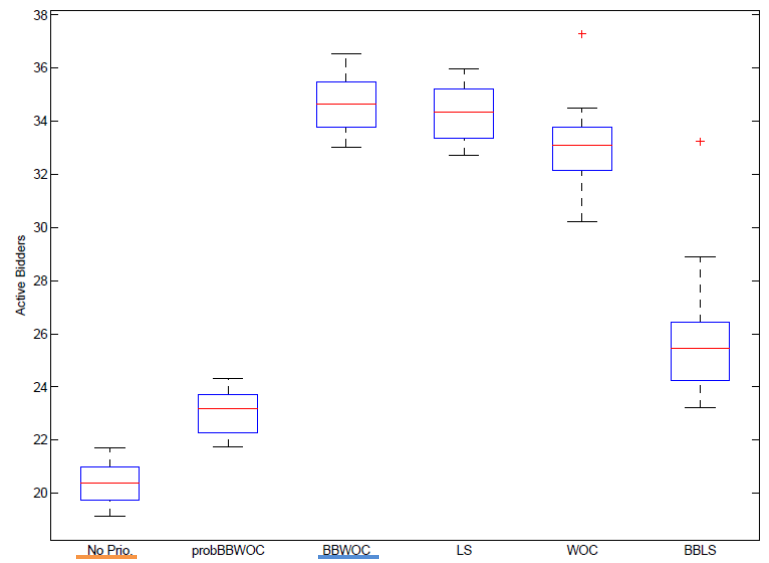
Mean Active Bidders Along Time



Mean Task Cost



expensive  
↑  
↓  
Ideal cost



# Conclusions




# Challenges vs. Contributions

1. Multi-attribute IC
  - PUMAA
    - Design of a multi-attribute auction for task allocation
    - Multi-criteria requirements study
2. Workflow related issues
  - FMAAC
    - Develop a framework for extending and customizing PUMAA
    - Study attribute types in auctions
3. Recurrent auctions' issues
  - Multi-dimensional fairness
    - Multidimensional-fairness mechanism for MARA.
    - Fair version of PUMAA
    - Minimize the bidder drop problem



# Conclusions: PUMAA

- Design auction mechanism for allocating multi-attribute resources in uncertain and dynamic workflow environments.

- PUMAA: *Published in:*
  - Suitable for uncertain domains PRIMA 2011 / AILOG 2010
  - Attributes considered along the whole mechanism STAIRS@ECAI 2012
  - Utility preservation
  - Incentive compatible CCIA 2013
- Evaluation function requirements  MDAI 2012
  - Monotonic, real-valued and bijective function
- Tested with a real data-based MAS simulator Journal of Intelligent Manufacturing (*in press*)



## Conclusions: FMAAC

- Classification of the attributes which can appear on multi-attribute auctions
  - Unverifiable bidder-provided
  - Verifiable bidder-provided
  - Auctioneer-provided
- Framework for multi-attribute auction customization
  - Generalization of PUMAA
  - Adaptation of the allocation to domain requirements
  - For instance: egalitarian allocations, trust-inclusion, etc.

*Published in:*

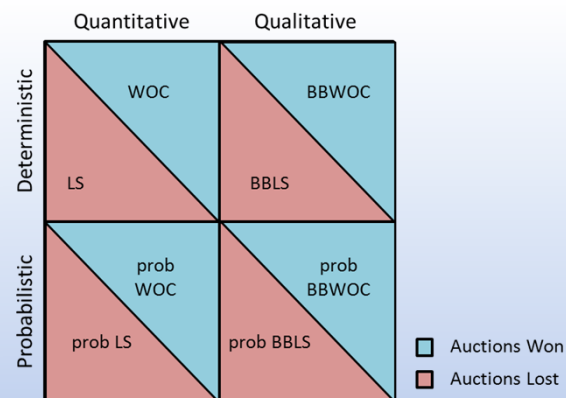
Expert Systems with Applications Journal 41(10), August 2014





# Conclusions: Multi-dimensional fairness

- Fairness in multi-attribute auctions must consider all the involved attributes.
- Definition of a fairness mechanism for multi-attribute auctions based on priorities.
  - Quantitative, Qualitative
  - Auctions won, Auctions lost
  - Deterministic, Probabilistic
- Experimentation showed that the use of priorities can minimize the bidder drop problem



Submitted to:

Knowledge-based Systems Journal (November 2013)

# Future works

- Generalize PUMAA for combinatorial auctions\*.
- Allow PUMAA to distinguish between “lies” and “estimation errors”.
- Use similarity measures to allow “Unstructured bids”.
- Add a trust-model to PUMAA using FMAAC\*.
- Adapt PUMAA to other domains such as the electricity smart grid or health-care management.
- Study how false-name bidding can affect the fairness mechanism.

\* [9] *Using multi-attribute combinatorial auctions for sustainable workflow scheduling*. F. Torrent, A. Pla, B. López. 12th Conference on Multiagent System Technologies (MATES 14). (To be submitted).



# Publications

- Journals

- **Albert Pla**, Pablo Gay, Joaquim Meléndez, Beatriz López [Petri net-based process monitoring: a workflow management system for process modelling and monitoring](#) In: Journal of Intelligent Manufacturing. 2012. pages 1-16 (pre-print).
- **Albert Pla**, Beatriz López, Javier Murillo, Nicolas Maudet [Multi-Attribute Auctions with Different Types of Attributes: Enacting Properties in Multi-Attribute Auctions](#) In: Expert Systems with Applications 41-10, August 2014, Pages 4829–4843
- **Albert Pla**, Beatriz López and Javier Murillo. Multidimensional [Fairness for Auction-based Resource Allocation](#). Knowledge-based Systems. (Submitted on November, 2013).

- Conferences

- B. Lopez, **Albert Pla**, D. Daroca, L. Collantes, S. Lozano, J. Meléndez. [Medical equipment maintenance support with service-oriented multi-agent services](#). PRIMA workshop on Services and Agents (ServAgents), Kolkata, India, November 12th-15th, 2010. To be published by Springer.
- **Albert Pla**, Beatriz López, Javier Murillo. [Multi-Attribute Auction Mechanism for Supporting Resource Allocation in Business Process Enactment](#), In: Proceedings of the Sixth Starting AI Researchers' Symposium (STAIRS 2012) at ECAI 2012. ISBN: 978-1-61499-095-6 pages: 228-239 Montpellier, France, August 2012



# Publications

- Conferences

- **Albert Pla**, Beatriz López, Javier Murillo. [Multi Criteria Operators for Multi-attribute Auctions](#). In The 9th International Conference on Modeling Decisions for Artificial Intelligence (MDAI 2012), Girona, Spain. November 2012. LNCS 7647, pp 318-328
- **Albert Pla**, Beatriz López, Javier Murillo [How to Demonstrate Incentive Compatibility in Multi-Attribute Auctions](#) In: Proc. 16th International Conference of the Catalan Association for Artificial Intelligence. Frontiers in Artificial Intelligence and Applications (vol 256). Pages: 303-306. October 2013, Vic, Catalonia
- Ferran Torrent, **Albert Pla** and Beatriz López. [Using multi-attribute combinatorial auctions for sustainable workflow scheduling](#). 12th Conference on Multiagent System Technologies (MATES 14). (To be submitted).

- Workshops

- **Albert Pla**, Beatriz López and Javier Murillo. [Workflow Resource Allocation through Auctions](#). 2nd Workshop on Artificial Intelligence and Logistics IJCAI, pp 55-60, Barcelona 2011.



# Grants & projects

- Scholarship
  - BR-UDG 12/2010
- Projects
  - AIMES: Advanced Infrastructure for Medical Equipment Management and Services
  - SUROS: Subastas Robustas mediante la incorporación de técnicas SMT
  - MoSHCA: My Mobile and Smart Health Care Assistant
- Journals
  - **Albert Pla**, Beatriz López, Pablo Gay, Carles Pous [eXiT\\*CBR.v2: Distributed case-based reasoning tool for medical prognosis](#) In: Decision Support Systems 54 (3), 1499-1510. DOI:10.1016/j.dss.2012.12.033. ISSN: 0167-9236
  - Pablo Gay, Beatriz López, **Albert Pla**, Jordi Saperas, Carles Pous [Enabling the Use of Hereditary Information from Pedigree Tools in Medical Knowledge-based Systems](#), Journal of Biomedical Informatics, Available online 15 June 2013, DOI:0.1016/j.jbi.2013.06.003. ISSN 1532-046



# Multi-Attribute Auctions: Application to Workflow Management Systems

Albert Pla Planas

Supervisors:

Dra. Beatriz López and Dr. Javier Murillo

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